

SCHEME OF EVALUATION
(Scoring Indicators)

Revision : 2015

Course Title : ENGINEERING MATHEMATICS II

Course Code : 2002

Qst No	Scoring Indicators	Split up	Sub Total	Total
	<u>PART-A</u>			
1.	Unit vector in the direction of $\vec{a} = \frac{\vec{a}}{ \vec{a} }$ $= \frac{3\hat{i} + 2\hat{j} - \hat{k}}{\sqrt{14}}$	1 1	2	
2.	$\begin{vmatrix} \sec\theta & \tan\theta \\ \tan\theta & \sec\theta \end{vmatrix} = \sec^2\theta - \tan^2\theta$ $= 1$	1 1	2	
3.	$A+B = \begin{bmatrix} 4 & 7 \\ 0 & 2 \end{bmatrix}$ $(A+B)^T = \begin{bmatrix} 4 & 0 \\ 7 & 2 \end{bmatrix}$	1 1	2	10
4.	$\int \sin^2 x \, dx = \int \left(\frac{1 - \cos 2x}{2} \right) dx$ $= \frac{1}{2} \left[x - \frac{\sin 2x}{2} \right] + c$	1 1	2	
5.	$dy = (4x + 5) dx$ $y = 4 \frac{x^2}{2} + 5x + c$	1 1	2	

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II 1.	<u>PART - B</u>			
	Let $\vec{a} = \hat{i} - 2\hat{j} + 3\hat{k}$ and $\vec{b} = 3\hat{i} - 2\hat{j} + \hat{k}$	2		
	$\vec{a} \cdot \vec{b} = 3 + 4 + 3 = 10$ $a = \sqrt{1 + 4 + 9} = \sqrt{14}$ $b = \sqrt{9 + 4 + 1} = \sqrt{14}$ $\theta = \cos^{-1} \left(\frac{\vec{a} \cdot \vec{b}}{ab} \right) = \frac{10}{14}$	1 1 1+1	6	
2.	Suppose that x^4 occurs in the $(r+1)^{\text{th}}$ term.			
	$t_{r+1} = {}^{15}C_r x^{n-r} a^r$	1		
	$= {}^{15}C_r (x^4)^{15-r} (-1/2)^r$	1		
	$= {}^{15}C_r (-1)^r x^{60-7r}$	2	6	
	$60 - 7r = 4, \quad r = 8$	1		
	Coefficient of $x^4 = {}^{15}C_8$	1		
3.	$\Delta = -3$	1		
	$\Delta_1 = -3$	1		
	$\Delta_2 = 3$	1		
	$\Delta_3 = 6$	1		
	$x = \frac{\Delta_1}{\Delta}, \quad y = \frac{\Delta_2}{\Delta}, \quad z = \frac{\Delta_3}{\Delta}$	1	6	
	$x = 1, \quad y = -1, \quad z = 2$	1		

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4.	$\det A = \begin{bmatrix} 3 & -2 & 3 \\ 2 & 1 & 7 \\ 4 & -3 & 2 \end{bmatrix}$ $ A = -17 \neq 0$ <p>Cofactor matrix of $A = \begin{bmatrix} -1 & -8 & -10 \\ -5 & -6 & 1 \\ -1 & 9 & 7 \end{bmatrix}$</p> $\text{adj}A = \begin{bmatrix} -1 & -5 & -1 \\ -8 & -6 & 9 \\ -10 & 1 & 7 \end{bmatrix}$ $A^{-1} = \frac{\text{adj}A}{ A }$ $= \frac{\begin{bmatrix} -1 & -5 & 1 \\ -8 & -6 & 9 \\ -10 & 1 & 7 \end{bmatrix}}{-17}$	<p>1</p> <p>2</p> <p>1</p> <p>1</p> <p>1</p>	6	
5	$\sin A \cos B = \frac{1}{2} [\sin(A+B) + \sin(A-B)]$ $\int \sin 3x \cos x \, dx = \frac{1}{2} \int (\sin 4x + \sin 2x) \, dx$ $= \frac{1}{2} \left[-\frac{\cos 4x}{4} - \frac{\cos 2x}{2} \right]$ $\int_0^{\pi/2} \sin 3x \cos x \, dx = \frac{1}{2} \left[-\frac{\cos 4\pi/2}{4} - \frac{\cos 2\pi/2}{2} \right]$ $+ \frac{\cos 0}{4} + \frac{\cos 0}{2}$ $= \frac{1}{2} \left[-\frac{1}{4} + \frac{1}{2} + \frac{1}{4} + \frac{1}{2} \right] = \frac{1}{2}$	<p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1+1</p>	6	

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6	$y = x^2$ and $y = 3x + 4$ $x^2 = 3x + 4$ $x = -1$ or 4 $A = \int_a^b (f(x) - \phi(x)) dx$ $= \int_{-1}^4 (x^2 - 3x - 4) dx$ $= \left[\frac{x^3}{3} - 3 \frac{x^2}{2} - 4x \right]_{-1}^4$ $= \left[\frac{64}{3} - 3 \times \frac{16}{2} - 4 \times 4 \right] - \left[-\frac{1}{3} - \frac{3}{2} + 4 \right]$ $= -\frac{125}{6} = \frac{125}{6} \text{ sq. units}$	 1 2 1 1 1	 6 	
7.	$\frac{dy}{dx} + Py = Q.$ $P = \tan x, Q = \sec x.$ Integrating factor, $If = e^{\int P dx}$ $= e^{\int \tan x dx}$ $= e^{\int \log \sec x} = \sec x.$ Solution is, $y \times If = \int Q If dx$ $y \times \sec x = \int \sec^2 x dx$ $y \times \sec x = \tan x + c$	 1 1 2 1 1	 6. 	

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III a	<p style="text-align: center;"><u>PART - C</u> <u>Unit - I</u></p> $\vec{a} + \vec{b} = 6\hat{i} + 2\hat{j} - 8\hat{k}$ $\vec{a} - \vec{b} = 4\hat{i} - 4\hat{j} + 2\hat{k}$ <p>If $(\vec{a} + \vec{b}) \cdot (\vec{a} - \vec{b}) = 0$, the vectors are perpendicular.</p> $(\vec{a} + \vec{b}) \cdot (\vec{a} - \vec{b}) = 24 - 8 - 16 = 0$	1 1 1 2	5	15
	<p>b.</p> $\vec{AB} = \hat{i} + \hat{j} + 6\hat{k}$ $\vec{AC} = -\hat{i} + \hat{j} + 3\hat{k}$ <p>Area of $\Delta ABC = \frac{1}{2} \vec{AB} \times \vec{AC}$</p> $\vec{AB} \times \vec{AC} = -3\hat{i} - 9\hat{j} + 2\hat{k}$ $ \vec{AB} \times \vec{AC} = \sqrt{94}$ $\text{Area} = \frac{1}{2} \sqrt{94}$	1 1 1 1 1	5	
	<p>c.</p> $(2x + 3y)^5 = (2x)^5 + 5C_1(2x)^4 3y + 5C_2(2x)^3 (3y)^2 + 5C_3(2x)^2 (3y)^3 + 5C_4(2x)(3y)^4 + (3y)^5$ $= 32x^5 + 5 \times 2^4 x^4 \times 3xy + 10 \times 2^3 x^3 \times 3^2 y^2 + 10 \times 2^2 \times 3^3 x^2 y^3 + 5 \times 2 \times 3^4 x y^4 + 3^5 y^5$ $= 32x^5 + 240x^4y + 740x^3y^2 + 1080x^2y^3 + 810xy^4 + 243y^5$	3 1 1	5	

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1V (a)	<u>OR</u>			
	$\frac{n}{2} + 1 = 7$ 7 th term is the middle term $t_{r+1} = {}^n C_r x^{n-r} a^r$ $t_7 = {}^{12} C_6 (2a)^6 (b/3)^6$ $= {}^{12} C_6 \frac{2^6 a^6 b^6}{3^6}$	1 1 2 1	5	
	b. Position vector of A = $3\hat{i} + 3\hat{j} + 3\hat{k}$ Position vector of B = $4\hat{i} - \hat{j} + 2\hat{k}$ $\vec{AB} = \text{P.V of B} - \text{P.V of A}$ $= \hat{i} - 4\hat{j} - \hat{k}$ Work done = $\vec{F} \cdot \vec{AB}$ $= 2 \times 1 + 1 \times -4 + 1 \times -1 = -3$	1 1 1 1 1	5	15
c. Moment of \vec{F} about O = $ \vec{OP} \times \vec{F} $ $\vec{OP} = \text{Position vector of P} - \text{Position vector of O.}$ $= (-2\hat{i} + 3\hat{j} + \hat{k}) - (\hat{i} + 2\hat{j} + 3\hat{k})$ $= -3\hat{i} + \hat{j} - 2\hat{k}$ $\vec{OP} \times \vec{F} = 3\hat{i} + \hat{j} - 4\hat{k}$ $ \vec{OP} \times \vec{F} = \sqrt{3^2 + 1^2 + (-4)^2}$ $= \sqrt{26} \text{ units.}$	1 1 1 1 1	5		

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Q1a	Unit - II				
	$a+3=2, a=-1$	2			
	$3a-2b=-7+2b, b=+1$	2	5		
	$a+b+c=8a, c=-8$	1			
(b)	$A^T = \begin{bmatrix} 1 & -2 & 3 \\ 0 & 1 & 2 \\ 5 & 6 & 7 \end{bmatrix}$	1			
	$A+A^T = \begin{bmatrix} 2 & -2 & 8 \\ -2 & 2 & 8 \\ 8 & 8 & 14 \end{bmatrix}$	1			
	$A-A^T = \begin{bmatrix} 0 & 2 & 2 \\ -2 & 0 & 4 \\ -2 & -4 & 0 \end{bmatrix}$	1			
	$(A+A^T)^T = \begin{bmatrix} 2 & -2 & 8 \\ -2 & 2 & 8 \\ 8 & 8 & 14 \end{bmatrix} = A+A^T$	1			
	$(A+A^T)^T = A+A^T, \therefore A+A^T$ is symmetric			5	
	$(A-A^T)^T = -\begin{bmatrix} 0 & 2 & 2 \\ -2 & 0 & 4 \\ -2 & -4 & 0 \end{bmatrix} = -(A-A^T)$	1			
	$\therefore A-A^T$ is skewsymmetric				

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C	$2A = \begin{bmatrix} 4 & 6 \\ 4 & 4 \end{bmatrix}$ $A = \begin{bmatrix} 2 & 3 \\ 2 & 2 \end{bmatrix}$ $B = A - \begin{bmatrix} 3 & 5 \\ 1 & 2 \end{bmatrix}$ $= \begin{bmatrix} 2 & 3 \\ 2 & 2 \end{bmatrix} - \begin{bmatrix} 3 & 5 \\ 1 & 2 \end{bmatrix}$ $= \begin{bmatrix} -1 & -2 \\ 1 & 0 \end{bmatrix}$	<p style="text-align: center;">1</p> <p style="text-align: center;">1</p> <p style="text-align: center;">1</p> <p style="text-align: center;">1</p>	5	
VII (a)	<p style="text-align: center;">Unit - III</p> $1. \int_0^1 \frac{1}{1+x^2} dx = [\tan^{-1}x]_0^1$ $= \tan^{-1}1 - \tan^{-1}0 = \pi/4$	<p style="text-align: center;">1</p> <p style="text-align: center;">1</p>	5	
	$2. \int (3x+4)(2x-1) dx = \int (6x^2+5x-4) dx$ $= \frac{6x^3}{3} + \frac{5x^2}{2} - 4x + C$	<p style="text-align: center;">1</p> <p style="text-align: center;">2</p>		
(b)	$\int \frac{4\cos x + 5}{\sin^2 x} dx = \int \frac{4\cos x}{\sin^2 x} dx + \int \frac{5}{\sin^2 x} dx$ $= 4 \int \frac{\cos x}{\sin x} \cdot \frac{1}{\sin x} dx + 5 \int \operatorname{cosec}^2 x dx$ $= 4 \int \cot x \operatorname{cosec} x dx + 5 \int \operatorname{cosec}^2 x dx$ $= 4 \operatorname{cosec} x - 5 \cot x + C$	<p style="text-align: center;">1</p> <p style="text-align: center;">1</p> <p style="text-align: center;">1</p> <p style="text-align: center;">2</p>	5	15

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C.	$\text{Put } u = x^3 + 3x, \quad du = (3x^2 + 3)dx$ $\frac{du}{3} = (x^2 + 1)dx$ $\int \frac{x^2 + 1}{x^3 + 3x} dx = \int \frac{1}{u} \frac{du}{3}$ $= \frac{1}{3} \log(x^3 + 3x)$ $\int_1^2 \frac{x^2 + 1}{x^3 + 3x} dx = \frac{1}{3} [\log(x^3 + 3x)]_1^2$ $= \frac{1}{3} [\log 14 - \log 4]$ $= \frac{1}{3} \log\left(\frac{14}{4}\right)$	<p style="text-align: center;">1</p>	5	
	<u>OR</u>			
VIII a.	$\cos^2 2x = \frac{1 + \cos 4x}{2}$ $\int \cos^2 2x dx = \int \frac{(1 + \cos 4x)}{2} dx$ $= \frac{1}{2} \left[x + \frac{\sin 4x}{4} \right] + c$ $\int_0^\pi \cos^2 2x dx = \frac{1}{2} \left[x + \frac{\sin 4x}{4} \right]_0^\pi$ $= \frac{1}{2} \left[\pi + \frac{\sin 4\pi}{4} - 0 - \frac{\sin 0}{4} \right]$ $= \frac{\pi}{2}$	<p style="text-align: center;">1</p>	5	

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b.	$\text{Let } \tan x = u, \quad du = \sec^2 x dx$ $\int \frac{\sec^2 x dx}{\sqrt{1 - \tan^2 x}} = \int \frac{du}{\sqrt{1 - u^2}}$ $= \sin^{-1} u + C$ $= \sin^{-1}(\tan x) + C$	<p style="text-align: center;">2</p> <p style="text-align: center;">1</p> <p style="text-align: center;">1</p> <p style="text-align: center;">1</p>	5	
c.	$\int x^2 \log x dx = \int \log x \cdot x^2 dx$ $= \log x \int x^2 dx - \int \left(\frac{d}{dx} \log x \cdot \int x^2 dx \right) dx$ $= \log x \frac{x^3}{3} - \int \left(\frac{1}{x} \times \frac{x^3}{3} \right) dx$ $= \log x \frac{x^3}{3} - \frac{1}{3} \frac{x^3}{3} + C$ $\int_0^2 x^2 \log x dx = \left[\frac{x^3}{3} \log x - \frac{1}{9} x^3 \right]_0^2$ $= \frac{8}{9} [3 \log 2 - 1]$	<p style="text-align: center;">1</p> <p style="text-align: center;">1</p> <p style="text-align: center;">1</p> <p style="text-align: center;">1</p>	5	15
<u>Unit - 4</u>				
IX a.	$\sin 3x = 0$ $\Rightarrow 3x = 0$ $\Rightarrow x = 0, \pi/3, 2\pi/3, \dots$ $\text{Area} = \int_a^b y dx$ $= \int_0^{\pi/3} \sin 3x dx$ $= \left[-\frac{\cos 3x}{3} \right]_0^{\pi/3}$ $= \left[-\frac{\cos 3\pi/3}{3} - \left(-\frac{\cos 0}{3} \right) \right] = \frac{2}{3}$	<p style="text-align: center;">1</p>	5	

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b.	$\text{Volume} = \pi \int_a^b y^2 dx$ $= \pi \int_0^4 4x dx$ $= \pi \cdot 4 \left[\frac{x^2}{2} \right]_0^4$ $= 32\pi \text{ cubic units.}$	1 2 1 1	5	15
c.	$\frac{dy}{dx} = e^{3x} \cdot e^{2y}$ $\frac{dy}{e^{2y}} = e^{3x} dx$ <p>Solution is, $\int \frac{dy}{e^{2y}} = \int e^{3x} dx$</p> $\frac{e^{-2y}}{-2} = \frac{e^{3x}}{3} + C$ $-\frac{e^{-2y}}{2} = \frac{e^{3x}}{3} + C$	1 1 1 2	5	
x a	<p style="text-align: center;"><u>OR</u></p> $\frac{x^2}{9} + \frac{y^2}{4} = 1$ $y=0 \Rightarrow \frac{x^2}{9} = 1, x = \pm 3$ $\text{Volume } V = \pi \int_a^b y^2 dx$ $= \pi \cdot \int_{-3}^3 \frac{4}{9} (9-x^2) dx$ $= \frac{4\pi}{9} \left[9x - \frac{x^3}{3} \right]_{-3}^3$ $= 16\pi \text{ cubic units.}$	1 1 1 1	5	

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(b)	$x \frac{dy}{dx} + 3y = 5x^2$ <p>Dividing the above equation by x</p> $\frac{dy}{dx} + \frac{3y}{x} = 5x$ <p>Integrating factor, $IF = e^{\int p dx}$</p> $= e^{\int \frac{3}{x} dx} = e^{3 \int \frac{1}{x} dx}$ $= e^{3 \log x} = x^3$ <p>Solution is, $Y \times IF = \int Q IF dx$</p> $y \times x^3 = \int 5x \cdot x^3 dx$ $y x^3 = 5 \cdot \frac{x^5}{5} + C$ $y x^3 = x^5 + C$	<p>1</p> <p>1</p> <p>2</p> <p>1</p> <p>1</p>	5	15
(c)	$\frac{d^2y}{dx^2} = \sec^2 x$ $\frac{dy}{dx} = \int \sec^2 x dx$ $= \tan x + C_1$ $y = \int (\tan x + C_1) dx$ $y = \log \sec x + C_1 x + C_2$	<p>2</p> <p>1</p> <p>1</p> <p>1</p>	5	