

(A)

SCHEME OF VALUATION

(Scoring Indicators)

Revision: 2015

Course code: 6044

Course Title: **DIGITAL SIGNAL PROCESSING**

Qst No	Scoring Indicator	Split Up Score	Sub Total	Total
<u>PART- A</u>				
1)	<p>A signal <math>x(n)</math> is said to be causal if its value is zero for <math>n &lt; 0</math>.</p> <p>eg: <math>x_1(n) = a^n u(n)</math>.</p> <p><math>x_2(n) = \{ \underset{\uparrow}{1}, 2, -3, -1, 2 \}</math></p>	1	2	
2)	<p>Let <math>x_1(n)</math> and <math>x_2(n)</math> are finite duration sequences both of length <math>N</math> with DFTs <math>X_1(K)</math> and <math>X_2(K)</math>. If <math>X_3(K) = X_1(K) \cdot X_2(K)</math>, then the sequence <math>x_3(n)</math> can be obtained by circular convolution defined as.</p> $x_3(n) = \sum_{m=0}^{N-1} x_1(m) \cdot x_2((n-m))_N$	1	2	
3)	<p>The Z-transform of a discrete time signal <math>x(n)</math> is defined as</p> $X(z) = \sum_{n=-\infty}^{\infty} x(n) \cdot z^{-n}$ <p>Where <math>z</math> is a complex variable, <math>z = r e^{j\omega}</math>.  <math>r</math> is the radius of the circle</p>	1	2	
4.	<p>FFT reduces the computation time required to compute discrete Fourier transform.</p> <p>FFT is based on decomposition and breaking the transform into smaller transforms and combining them to get total transform.</p>	1	2	

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S.	TMS320C3x, TMS320C67x, ADSP-21xx	2	2	
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Part-B

II.1) Scalar Multiplication.

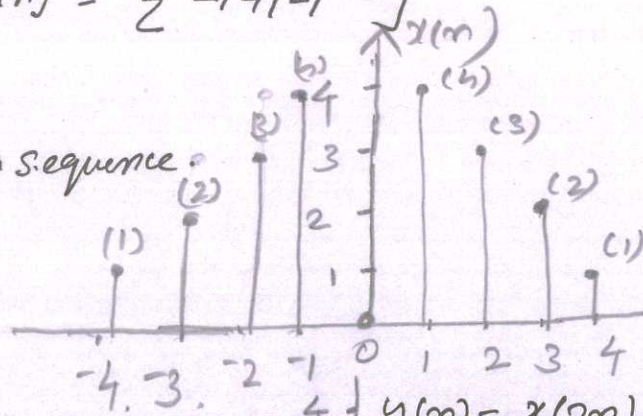
Here the signal  $x(n)$  is multiplied by a scalar factor  $a$ .

$$x(n) \xrightarrow{a} y(n) = a \cdot x(n).$$

eg: if  $x(n) = \{1, 2, 1, -1\}$  and  $a = 2$ . Then the signal  $ax(n) = \{2, 4, 2, -2\}$

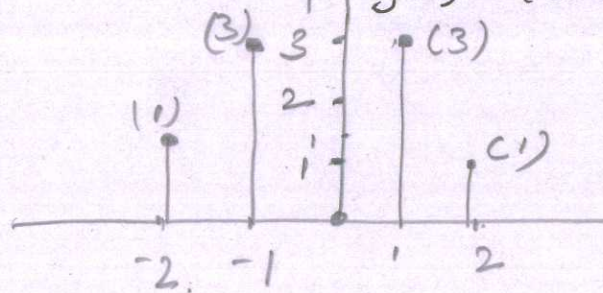
Time Scaling.

Let  $x(n)$  be a sequence



$x(2n)$

$y(0) = x(0) = 0$   
 $y(1) = x(2) = 1$   
 $y(2) = x(4) = 1$   
 and soon.



3

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2)	<p align="center"><u>Unit step signal</u></p> $X(z) = \sum_{n=-\infty}^{\infty} x(n) \cdot z^{-n}$ $x(n) = u(n), \quad X(z) = \sum_{n=0}^{\infty} z^{-n}$ $u(n) = \begin{cases} 1, & \text{for } n > 0 \\ 0, & \text{for } n < 0 \end{cases} \Rightarrow X(z) = \sum_{n=0}^{\infty} z^{-n}$ $= \frac{1}{1-z^{-1}} = \frac{z}{z-1}$ $X(z) = \frac{z}{z-1}$ <p align="center"><u>Unit impulse signal</u></p> $X(z) = \sum_{n=-\infty}^{\infty} x(n) \cdot z^{-n}, \quad X(z) = \sum_{n=-\infty}^{\infty} 1$ $X(z) = \underline{\underline{1}}$ $\delta(n) = \begin{cases} 1, & \text{for } n = 0 \\ 0, & \text{otherwise.} \end{cases}$	3	6	
3)	<p>→ Decimation in time algorithm is used to calculate the DFT of a N point sequence.</p> <p>→ The idea is to break the N point sequence into two sequences.</p> <p>→ Then the DFTs of which can be combined to give the DFT of the original N point sequence.</p> <p>→ The N point sequence is divided into two <math>\frac{N}{2}</math> point sequences <math>x_e(n)</math> and <math>x_o(n)</math></p>	1	1	1

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	<p>→ which have Even and Odd members of <math>x(n)</math> respectively.</p> <p>→ The <math>N/2</math> point DFTs of these two sequences are evaluated and combined to give the <math>N</math> point DFTs</p> <p>4) Given <math>x_1(n) = \{2, 2, 1, 2\}</math>, <math>x_2(n) = \{-2, -1, 3, 2\}</math>.</p> <p>(a) <math>x_1(n) + x_2(n) = \{2-2, 2-1, 1+3, 2+2\}</math>  <math>= \{0, 1, 4, 4\}</math>.</p> <p>(b) <math>x_1(n) \times x_2(n) = \{2 \times -2, 2 \times -1, 1 \times 3, 2 \times 2\}</math>  <math>= \{-4, -2, 3, 4\}</math>.</p> <p>50) Rectangular Window.</p> $w_R(n) = 1, \text{ for } -\frac{(N-1)}{2} \leq n \leq \frac{(N-1)}{2}$ $= 0, \text{ otherwise.}$	1	6	6

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② Triangles or Bartlett window.

$$w_T(n) = 1 - \frac{2|m|}{N-1}, \text{ for } -\frac{(N-1)}{2} \leq n \leq \frac{(N-1)}{2}$$

0, otherwise.

③ Hamming Window.

$$w_{Hm}(n) = 0.5 + 0.5 \cos \frac{2\pi n}{N-1}, \text{ for } -\frac{(N-1)}{2} \leq n \leq \frac{(N-1)}{2}$$

0, otherwise.

④ Hamming Window.

$$w_H(n) = 0.54 + 0.46 \cos\left(\frac{2\pi n}{N-1}\right)$$

for  $-\frac{(N-1)}{2} \leq n \leq \frac{(N-1)}{2}$

0, otherwise.

⑤ Blackman window.

$$w_B(n) = 0.42 + 0.5 \cos \frac{2\pi n}{N-1} + 0.08 \cos \frac{4\pi n}{N-1}$$

for  $-\frac{(N-1)}{2} \leq n \leq \frac{(N-1)}{2}$ .

0, otherwise.

(Any 3)  
Each carry 2 marks.  
3x2

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	<p>6) Raised Cosine Window.</p> $w_{\alpha}(n) = \alpha + (1-\alpha) \cos \frac{2\pi n}{N-1} \text{ for } -\frac{(N-1)}{2} \leq n \leq \frac{(N-1)}{2}$ <p>0, otherwise.</p>		6
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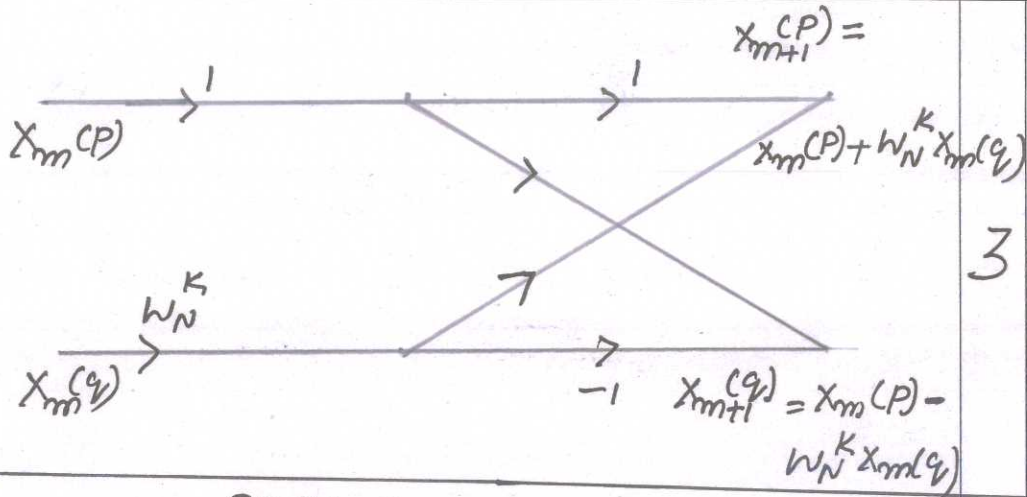
6)	<p>Applications of DSP.</p> <ol style="list-style-type: none"> <li>① Telecommunication</li> <li>② Instrumentation and Control.</li> <li>③ Audio Signal processing.</li> <li>④ Military.</li> <li>⑤ Medicine.</li> <li>⑥ Image Processing.</li> </ol>	<p>1 1 1 1 1 1</p>	6
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7)	<p>Basic butterfly diagram of DIT algorithm.</p> <p> <math>X_{m+1}(P) = X_m(P) + W_N^K X_m(Q)</math>  <math>X_{m+1}(Q) = X_m(P) - W_N^K X_m(Q)</math> </p>		3
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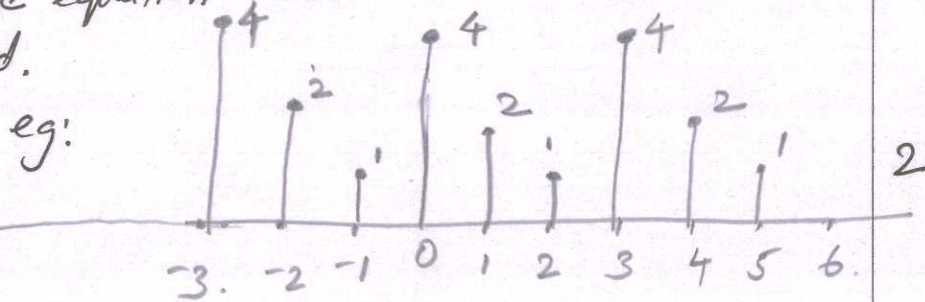
36

PART - C  
UNIT - I

III (a) Periodic Signal.

- A discrete-time signal  $x(n)$  is said to be periodic with period  $N$  if and only if  $x(N+n) = x(n)$  for all  $n$ .

- The smallest value of  $N$  for which the above equation holds is known as fundamental period.



Periodic Signal.

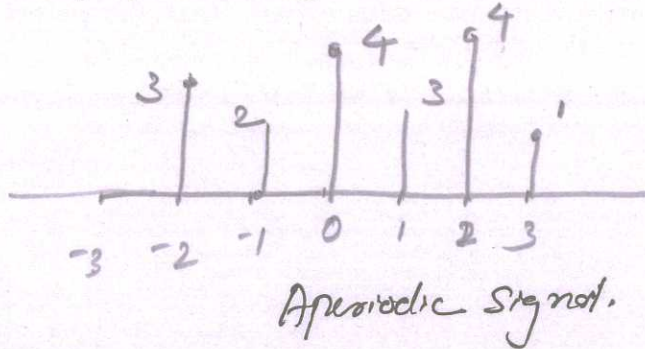
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Aperiodic Signal.

Signals which does not obey the equation  $x(N+n) = x(n)$  for all  $n$  are aperiodic.



2  
8  
2

(b) Given  $y(n) = x(n) + 2(n-1)$ .

(i)

$$y(n) = T[x(n)] = x(n) + x(n-1)$$

If the input is delayed by  $K$  units in time

$$y(n, K) = T[x(n-K)] = x(n-K) + x(n-K-1)$$

If we delay the output by  $K$  units in time

$$\text{then } y(n-K) = x(n-K) + x(n-K-1)$$

$\Rightarrow y(n, K) = y(n-K)$ .  $\therefore$  The System is TIME INVARIANT.

(ii)  $y(n) = x(-n)$ .

$$\text{Given } y(n) = T[x(n)] = x(-n)$$

If the input is delayed by  $K$  units in time and applied to the S/m.

$$y(n, K) = T[x(n-K)] = x(-n-K)$$

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If the output is delayed by  $k$  samples.  
 $y(n-k) = x(-(n-k)) = x(-n+k)$   
 $\Rightarrow y(n+k) \neq y(n-k)$ .  
 $\therefore$  The system is TIME VARIANT.

3 7

1Vca) (i) Given  $y(n) = x(n) + \frac{1}{x(n-1)}$

$$y_1(n) = T[x_1(n)] = x_1(n) + \frac{1}{x_1(n-1)}$$

$$y_2(n) = T[x_2(n)] = x_2(n) + \frac{1}{x_2(n-1)}$$

O/p due to weighted sum of inputs.

$$y_3(n) = T[a_1 x_1(n) + a_2 x_2(n)]$$

$$= a_1 x_1(n) + a_2 x_2(n) + \frac{1}{a_1 x_1(n-1) + a_2 x_2(n-1)}$$

Also, linear combination of two o/p.

$$a_1 y_1(n) + a_2 y_2(n) = a_1 x_1(n) + \frac{a_1}{x_1(n-1)} + a_2 x_2(n) + \frac{a_2}{x_2(n-1)}$$

Since  $y_3(n) \neq a_1 y_1(n) + a_2 y_2(n)$ .

System is NON LINEAR. as superposition principle is not satisfied.

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	<p>(i) <math>y(n) = n x(n)</math>.</p> <p><math>y_1(n) = n x_1(n), y_2(n) = n x_2(n)</math>.</p> <p>Weighted Sum of outputs is .</p> <p><math>a_1 T[x_1(n)] + a_2 T[x_2(n)] = a_1 n x_1(n) + a_2 n x_2(n)</math>.</p> <p>Now o/p due to weighted sum of inputs .</p> <p><math>y_3(n) = T[a_1 x_1(n) + a_2 x_2(n)] = n a_1 x_1(n) + n a_2 x_2(n)</math></p> <p><math>\Rightarrow y_3(n) = a_1 y_1(n) + a_2 y_2(n)</math></p> <p>Superposition principle is satisfied Hence the system is <b>LINEAR</b>.</p>	5		
			10	

	<p>(b) <u>Shifting</u>.</p> <p>The shift operation takes the input sequence and shifts the values by an integer increment of the independent variable.</p> <p><math>y(n) = x(n-k)</math></p> <p>The shifting may delay or advance the sequence in time.</p> <p><u>Time Reversal</u> It is obtained by folding the sequence about <math>n=0</math>.</p> <p><math>y(n) = x(-n)</math></p> <p><u>Time Scaling</u> <math>y(n) = x(\lambda n), \lambda = 0 \text{ to } \infty</math>.</p> <p>eg: <math>y(n) = x(2n)</math></p>	1		
		1		
			5	
		1		

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<p>V (a)</p>	<p align="center"><u>Unit - II</u></p> $X(K) = \sum_{n=0}^{N-1} x(n) \cdot e^{-j2\pi nK/N}, K=0,1,\dots,N-1$ <p align="center"><math>N=4</math></p> $X(0) = \sum_{n=0}^3 x(n) = x(0) + x(1) + x(2) + x(3)$ $X(1) = \sum_{n=0}^3 x(n) \cdot e^{-j\pi n/2} = \underline{-j}$ $ X(1)  = \underline{1}$ $X(2) = \sum_{n=0}^3 x(n) \cdot e^{-j2\pi n} = 1,  X(2)  = 1$ $X(3) = \sum_{n=0}^3 x(n) \cdot e^{-j3\pi n/2} = j,  X(3)  = 1$ $X(K) = \{ \underline{3}, \underline{-j}, \underline{1}, \underline{j} \},  X(K)  = \{ \underline{3}, \underline{1}, \underline{1}, \underline{1} \}$	<p align="center">1 2 2 2 1</p>	<p align="center">8</p>
<p>1b)</p>	<p>If two finite duration sequences <math>x_1(n)</math> and <math>x_2(n)</math> are linearly combined as.</p> $x_3(n) = a x_1(n) + b x_2(n)$ <p>Then the DFT of <math>x_3(n)</math>, <math>X_3(K) = a X_1(K) + b X_2(K)</math></p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <math display="block">\text{DFT} [a_1 x_1(n) + a_2 x_2(n)] = a_1 X_1(K) + a_2 X_2(K)</math> </div>	<p align="center">4 3</p>	<p align="center">7</p>

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V1(a)	$X(z) = \frac{1}{1+4.5z^{-1}+3.5z^{-2}},  z  > 3.5$ $= \frac{z^2}{z^2+4.5z+3.5}, \quad \frac{X(z)}{z} = \frac{z}{z^2+4.5z+3.5}$ $\frac{X(z)}{z} = \frac{z}{(z+1)(z+3.5)} = \frac{A}{z+1} + \frac{B}{z+3.5}$ $A = (z+1) \cdot \frac{z}{(z+1)(z+3.5)} \Big _{z=-1} = \frac{-1}{2.5} = \underline{\underline{-\frac{2}{5}}}$ $B = (z+3.5) \cdot \frac{z}{(z+1)(z+3.5)} \Big _{z=-3.5} = \underline{\underline{\frac{7}{5}}}$ $X(z) = \frac{-2}{5} \cdot \frac{1}{z+1} + \frac{7}{5} \cdot \frac{1}{z+3.5}$ $x(n) = -0.4(-1)^n u(n) + 1.4(-3.5)^n u(n)$	2 2 3 <del>12</del> 2	10	
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(b)	<p>Given <math>x(n) = \{1, 0, 3, -1, 2\}</math>.</p> $X(z) = \sum_{n=-\infty}^{\infty} x(n) \cdot z^{-n}$ $X(z) = 1 + 3z^{-2} - z^{-3} + 2z^{-4}$	2 3	5	
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UNIT - III

The computation of 8 point DFT using radix 2 FFT involves three stages of computation. The given 8 point sequence is decimated to 2 point sequences. For each 2 point sequence, the 2 point DFT is computed. From the results of 2 point DFT 4 point DFT can be computed. From the result of 4 point DFT, the 8 point DFT can be computed.  $x(n)$  is in bit reversed order.

VIII(a)			6	
			8	
			2	



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VIII(a)

$$X(K) = \{ 12, 1-j2.414, 0, 1-j0.4142, 0, 1+j0.4142, 0, 1+j2.414 \}$$

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VIII (b) 8 point FFT using radix-2 DIF butterfly diagram.

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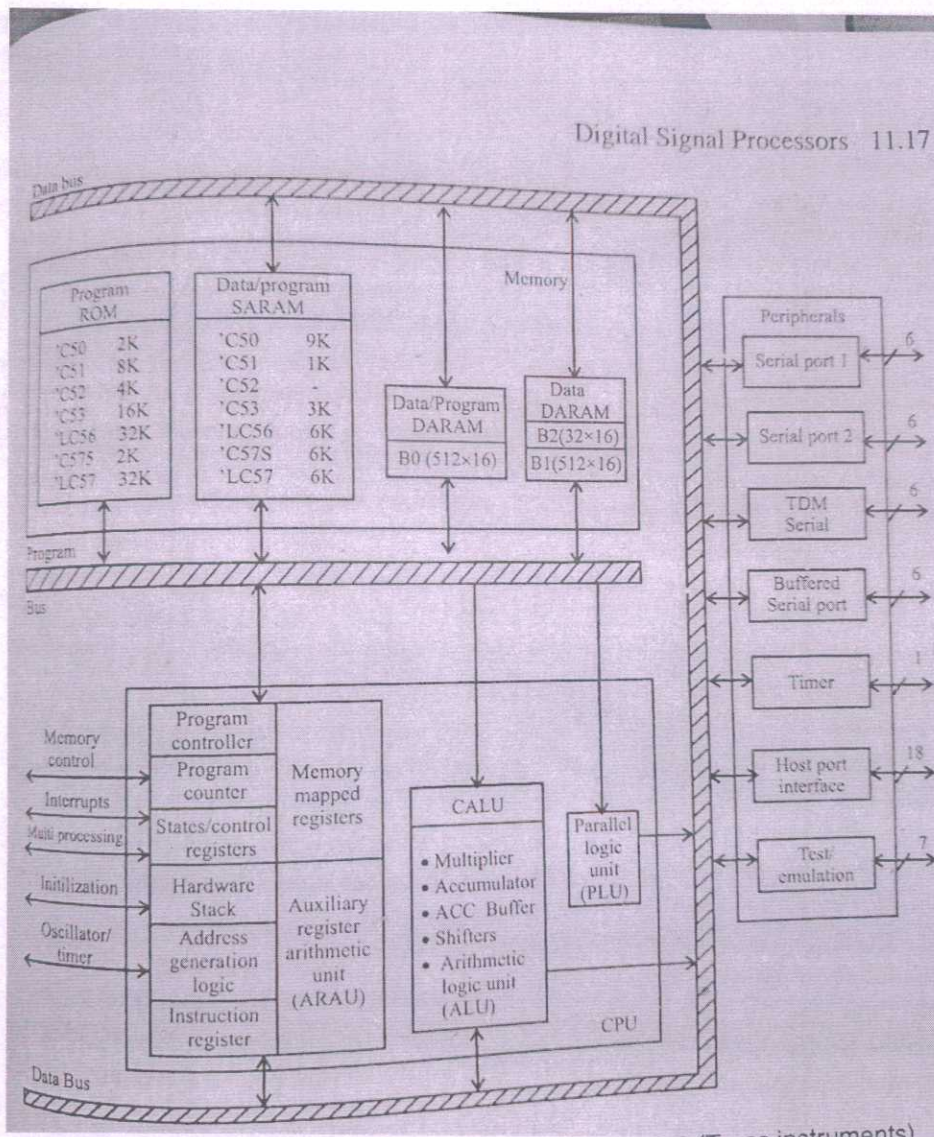
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1x10) **TMX320C50 DSP Architecture.**



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1x6)	<p>Advantages of Digital filters.</p> <ul style="list-style-type: none"> <li>→ Unlike analog filter, the digital filter performance is not influenced by component ageing, temperature and power supply variations.</li> <li>→ They are highly immune to noise and possess considerable parameter stability.</li> <li>→ Multiple filtering is possible only in digital filter.</li> <li>→ No problems of input or output impedance matching with Digital filters.</li> <li>→ Coefficients of Digital filter can be programmed and altered any time to obtain the desired characteristics.</li> </ul>	1 1 1 1 1	5	
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X(a)	<p>Addressing Modes.</p> <p>The addressing modes of TMS320C50 are</p> <ol style="list-style-type: none"> <li>① Immediate Addressing.</li> <li>② Indirect addressing.</li> <li>③ Register addressing.</li> <li>④ Memory mapped register addressing.</li> <li>⑤ Direct addressing.</li> <li>⑥ Circular addressing.</li> </ol> <p>Seven types of Indirect addressing.</p> <ol style="list-style-type: none"> <li>① Auto increment.</li> <li>② Auto decrement</li> <li>③ Post indexing by adding the contents of ARO.</li> <li>④ Post indexing by subtracting the contents of ARO.</li> <li>⑤ Single indirect addressing with no increment.</li> <li>⑥ Single indirect addressing with no decrement</li> <li>⑦ Bit reversal addressing.</li> </ol>	6		10
		2	4	

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XCB)	→ Architectural Features.	2	5	
	→ Execution Speed	1		
	→ Type of Arithmetic	1		
	→ Word length.	1		

2009 20  
6